

1 A New Ranking Algorithm for a Round-Robin Tournament

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5

6 **Abstract**

7 The problem of ranking players in a round- robin tournament, in which outcome of any match
 8 is a win or a loss, is to rank players according to their performances in the tournament. In this
 9 paper, we have improved previously developed MST (Majority Spanning Tree) algorithm for
 10 solving this problem, where the number of violations has been chosen as the criterion of
 11 optimality. We have compared the performance of our algorithm with the MST algorithm and
 12 GIK algorithm.

13

14 **Index terms**— ranking, round-robin tournament, upset, digraph, MST, GIK.15 **1 I. Introduction**

16 The problem of ranking players in a tournament has been the subject of various research investigations. This
 17 tournament structure also arises in other environments like the problems of soliciting customer preferences of a
 18 set of products, establishing funding priorities of a set of projects [5], establishing searching priorities for a set of
 19 search engines in the internet. It is known that the results of a tournament can be represented in a digraph, $G=(V,$
 20 $A)$ known as tournament graph, where vertices correspond to players and arcs correspond to match results. A
 21 tournament result is said to be upset (or violation) if a lowly-ranked player has defeated a highly-ranked player.
 22 Ali [1], Cook [6], Goddard [5], Poljak [3] and many others have concentrated on the problem of determining ranks
 23 based on the results of the tournament. A constructive lower bound on the tournament ranking function was
 24 obtained in [4]. In [2], a heuristic solution to optimize the number of violations has been developed. This paper
 25 presents a new version of MST algorithm which reduces the number of violations compared to MST algorithm.
 26 The problem of minimizing the number of upsets is equivalent to finding the minimum number of arcs in a digraph
 27 deletion of which results in an acyclic digraph.

28 **2 II. Preliminaries**

29 Before describing the new algorithm, we present here a brief discussion on MST algorithm [2] and GIK algorithm
 30 [1]. MST: For ease of discussion we recapitulate some of the definitions used in MST algorithm.

31 1. $\text{cutset}(i, k, j)$ -is the difference between the numbers of outgoing arcs from set (i, k) to set $(k + 1, j)$ and
 32 outgoing arcs from set $(k + 1, j)$ to set (i, j) , where set (i, j) is the set of vertices corresponding to players ranked
 33 from i to j . 2. $\text{maxwin}(i, j)$ -is the maximum number of wins of a player in set (i, j) . 3. $\text{pair}(i, j)$ -corresponds to
 34 an upset if the player ranked j defeats the player ranked i . MST () Repeat until swap = false swap ?false for $i = 1$
 35 to size-1 do for $j = i + 1$ to size do for $k=i$ to $j-1$ do if $\text{cutset}(i,k,j) < 0$ swap ?true elseif $\text{cutset}(i,k,j) = 0$ if $\text{pair}(i,j)$
 36 or $(i - 1, k + 1)$ or $(k, j + 1)$ is upset then swap ? true swap respective pair else if $\text{maxwin}(i, k) < \text{maxwm}(k +$
 37 $1, j)$ swap respective pair endif endif if swap = true then swap set $(\{i, k\}, \{k + 1, j\})$ © 2017 Global Journals Inc.
 38 (US) ()

39 **3 G**

40 This problem is known as Minimum Feedback Arc set Problem, and is NP-hard for general digraphs [1].

41 Assuming the number of players in the tournament to be n , complexity of the MST algorithm can be derived
 42 as follows: In the k -loop, calculation of cutset value requires $O(n)$ operations. Each of the i, j and k -loop will

11 IV. EXPERIMENTAL RESULTS

43 be done at most n times for a single swap, which will reduce the number of violations by 1. The amount of
44 computation for this is at most $O(n^4)$. Since there can be at most $O(n^2)$ violations initially, the algorithm
45 requires at most $O(n^6)$ calculations.

46 4 GIK: This algorithm is based on the IK algorithm [].

47 When applying the IK algorithm to rank a tournament, two basic steps are executed in case of a tie. The first
48 attempts to break the tie by restoring the players, while the second (which is applied when the first step fails)
49 randomly ranks the players involved in the tie. The GIK algorithm differs from the IK procedure in these two
50 steps. The restoring method is different, and if this restoring method does not resolve the ties, an attempt is
51 made to rank the players in a manner that will reduce the overall number of violations.

52 The GIK algorithm appears below. $> \dots > P_k$) and $R_i = (Q_1 > Q_2 > \dots > Q_J$, then $R1||R2 = (P_1 > P_2 > \dots > P_k > Q_1 > Q_2 > \dots > Q_J$).

54 5 The GIK Algorithm

55 Let $R = \{P_i\}$, $A = \{P_i\}$

56 6 III. THE NEW ALGORITHM

57 In this Section we propose A new version of MST algorithm that results in minimum number of upset compared
58 to the MST algorithm and GIK algorithm for ranking players in a round-robin tournament [].

59 We consider only simple connected digraphs $G = (V, A)$. Spanning trees of any digraph are denoted by T . A
60 directed cutset(V_i, V_j) is defined as $\{(k, l) | k \in V_i, l \in V_j\}$

61 For improvement of the algorithm we introduce the following symbols and functions: S_a -start of set A E_a -end
62 of set A S_b -start of set B E_b -end of set B S_c -start of set C E_c -end of set C $Cutset(A, B)$ -is the difference between
63 the numbers of outgoing arcs from set A to set B and outgoing arcs from set B to set A .

64 $Cutset(A, C)$ -is the difference between the numbers of outgoing arcs from set A to set C and outgoing arcs
65 from set B to set A .

66 $Cutset(B, C)$ -is the difference between the numbers of outgoing arcs from set B to set C and outgoing arcs
67 from set C to set B .

68 Procedure: Improved MST 3.

69 7 4.

70 5.

71 8 6.

72 7. 8.

73 9 9.

74 10.

75 10 11.

76 12. 13.

77 14. 15. 16.

78 11 IV. Experimental Results

79 The new_MST Algorithm has been compared with MST Algorithm and the GIK algorithm on the basis of a set
80 of randomly generated tournaments of sizes ranging from 5 to 50 players. All algorithms have been programmed
81 in C and runs were made on a core i3 machines. We have been measured both in terms of violations and
82 computational time. Here new_MST gives better result compared to MST and GIK with respect to number of
violations. ¹

Figure 1:

83

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and $D = D \setminus \{P_i\}$. If $|D| = \text{á}'?"$, then go to (2). Otherwise go to (4).

Let $i=i+1$, and go to (12).

Execute procedure *Arrange* on the ranking R .

End.

If $A = \text{á}'?"$, then go to (15); otherwise determine the current scores of players in A .

If $A = \text{á}'?"$, then go to (15); otherwise determine D , the dominant set.

If $|D| > 1$, then go to (6).

Letting P denote the only player in D , form the ranking $R = R \parallel P$, let $A = A \setminus \{P\}$ and go to (3).

If from the last time of updating the current scores of A [step (2)], set A has changed, then go to (2).

[*Note: 1, P 2, . . . , P n*}. If $|D| > 2$, then go to (9). Let P_1 and P_2 , denote the players in D with $P_1 > P_2$. Let $R = R \parallel P_1 \parallel P_2$, and $A = A \setminus \{P_1, P_2\}$. Go to (2). If $R = \text{á}'?"$, then go to (11).]

Figure 2:

1

No of player	Initial upset	GIK	MST	New MST
5	3.66	2.66	1.66	1.66
10	24.00	13.33	9.00	8.66
15	47.33	39.33	25.66	24.66
20	89.00	38.33	25.33	22.00
25	194.33	109.66	76.33	72.33
30	106.66	94.66	67.33	61.00
40	482.00	138.66	88.66	79.00
50	585.66	515.00	439.00	418.33

Figure 3: Table 1 :

2

No of player	GIK	MST	New MST	
5	0.0013	0.0030	0.0010	
10	0.0103	0.0090	0.0110	
15	0.0173	0.0093	0.0680	
20	0.0226	0.0236	0.5756	
25	0.0266	0.0563	88.5506	
30	0.0320	0.0216	1268.37	
40 50	0.043 0.054	V. Conclusion 0.1913 4.147	24877.110 63415.8188	Year 2017

[Note: GThis page is intentionally left blank]

Figure 4: Table 2 :

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