

1 Two-Party Threshold Key Agreement Protocol for Manets using 2 Pairings

3 Ch. Asha Jyothi¹, G. Narsimha², J. Prathap³ and Gorti VNKV Subba Rao⁴

4 ¹ JNTUH College of Engineering Jagtial

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6

7 **Abstract**

8 In MANET environment, the nodes are mobile i.e., nodes move in and out dynamically. This
9 causes difficulty in maintaining a central trusted authority say Certification Authority CA or
10 Key Generation Centre KCG. In addition most of cryptographic techniques need a key to be
11 shared between the two communicating entities. So to introduce security in MANET
12 environment, there is a basic need of sharing a key between the two communicating entities
13 without the use of central trusted authority. So we present a decentralized two-party key
14 agreement protocol using pairings and threshold cryptography ideas. Our model is based on
15 Joux's three-party key agreement protocol which does not authenticate the users and hence is
16 vulnerable to man-in-the-middle attack. This model protects from man-in-the-middle attack
17 using threshold cryptography.

18

19 **Index terms**— pairing-based cryptography, threshold cryptography, bilinear maps, mobile ad hoc networks,
20 key agreement protocol.

21 Introduction and so on. Security [22] is considered to be the major "barrier" in the commercial use of this
22 technology. Security is indeed one of the most difficult problems to be solved in these networks due to lack of
23 centralized network management. Most of the security mechanisms essentially require a secret key or session key
24 or master key to be shared between the two communicating entities. So there is a need to share a key between
25 the sender and receiver without the use of centralized network management or certification authority.

26 Key agreement is one of the basic cryptographic essentials. This is needed in cases where two or more users
27 want to communicate securely among themselves. The first two-party key sharing protocol was introduced by
28 Diffie-Hellman. Since its detection in 1976, the Diffie-Hellman protocol [1] has become one of the most well-known
29 and mostly used cryptographic primitive. In its basic version, it is an efficient solution to the problem of creating
30 a common secret between two participants. Since this protocol is also used as a building block in many complex
31 cryptographic protocols, finding a generalization of Diffie-Hellman would give a new tool and might lead to new
32 and more efficient protocols. But this is an unauthenticated protocol in the sense that an adversary who has
33 control over the communication channel can use the man-in-the-middle attack to share two separate keys with
34 the two users, without the users being aware of this. In this paper, we present a secure two-party key agreement
35 protocol that protects from man-in-the-middle attack. Our protocol is based on Joux's protocol [1] which in turn
36 is the generalization of Diffie-Hellman protocol.

37 One round tripartite key agreement Joux's protocol [1] uses Weil and Tate Pairings and the idea of Diffie-
38 Hellman. These pairings were first used in cryptology as cryptanalysis tools to decrease the complexity of the
39 discrete logarithm problem on some "weak" elliptic curves, but they are also used today to build cryptographic
40 systems.

41 In this paper, we present a secure two-party key agreement protocol for MANET environment. This model
42 extends the popular known Joux's tripartite key agreement protocol [1] to two-partite with minor modifications.
43 Similar to Joux model [1], this model uses pairings or bilinear maps, unlike Joux this model uses threshold
44 cryptography.

45 **1 Recently**

46 Pairing-based wireless technology [22] is suitable of communicating virtually every location on the plane of the
47 earth. Most of the people exchange information every day using pagers, cellular telephones, laptops, several types
48 of personal digital assistants (PDAs) and other wireless communication products. A Mobile Ad hoc NETwork
49 (MANET) is one that comes into practice as needed, without the support of existing infrastructure or any other
50 kind of fixed stations. MANET is an independent system of mobile hosts (also serving as routers), connected
51 by wireless links. In a MANET, no infrastructure exists and the network topology may dynamically change
52 in an unpredictable manner since nodes are free to move. The important natural characteristics of MANETs
53 [22] include frequently changing Topology, Lack of Central Administration, Battery Power supply or Restricted
54 Energy, Restricted bandwidth, Physical Security fear.

55 Ad hoc networks are particularly prone to malicious behavior. Lack of any centralized network management or
56 certification authority makes these dynamically changing wireless structures extremely vulnerable to penetration,
57 eavesdropping, interference, W Year 2015 cryptography in the form of Identity-based cryptography has become
58 a highly working research issue.

59 The paper is organized as: Section II discusses on the background fundamentals needed to understand the
60 proposed model. Section III discusses on the previous work done to share a key between two entities using
61 pairings. Section IV talk about the detailed description of the proposed model. Section V gives the software
62 implementation of the proposed model and Section VI confers the conclusion and future enhancements that can
63 be done to improve the model.

64 **2 II.**

65 **3 Preliminaries a) Bilinear Maps**

66 The bilinear map was proposed originally as a tool for attacking elliptical curve encryption by reducing the
67 problem of discrete algebra on an elliptical curve to the problem of discrete algebra in a finite field, thereby
68 reducing its complexity. However, this method has been used recently as an encryption tool for information
69 protection, instead of an attacking tool. Bilinear pairing is equivalent to a bilinear map.

70 Consider two additively written abelian groups A_1 and A_2 ; the identity element being 0. Also consider a
71 multiplicatively written cyclic group C ; the identity element being 1. A pairing [2][17] on A_1 , A_2 and C is a
72 non-degenerate, bilinear map e is a function which maps a pair of points on an elliptic curve E ,
73 defined over fields A_1 and A_2 , to an element of the multiplicative group of a finite extension field C . This mapping
74 is said to be pairing as it maps a pair of elliptic curve points. The pairing e has the following characteristics:
75 Non-degenerate: Given a point the re e xis ts a point s uch tha t e ; Whe re is the p oint at infinity on the elliptic
76 curve over the finite field A_1 .

77 **4 Bilinear: for all points**

78 This can be redefined in the following way:

79 Computable: There exists a computationally efficient algorithm to find $e(X, Y)$ for all X Laws of Bilinear
80 Pairings: The following equations holds good for the bilinear pairing e . Consider X is the p oint at a t Infinity.
81 where and C are cyclic groups of prime order p written additively and multiplicatively respectively.

82 The second type of pairing called Asymmetric Pairings are of the form The first form is just the special case
83 with $A_2 = A_1$. Asymmetric Pairings are further divided into two types and hence leading to totally three types
84 of Pairings [19] Type 1: $A_1 = A_2$ Symmetric Pairing; Type 2 :

85 As ymmetric Pa iring but there is a n efficiently computable homomorphism function Type 3 :
86 Asymmetric Pairing and there are no efficiently computable homomorphism functions between A_1 and A_2 .

87 **5 b) Threshold Cryptography**

88 Let t and n be positive integers, t threshold scheme [25] is a method of sharing a secret K among a set of n
89 participants in such a way that any t participants can compute the value of the secret, but no group of $t+1$ or
90 fewer can do so.

91 Let the set of participants be denoted by E . The value of the secret K is chosen by the dealer, denoted D , who
92 is a special participant not in E . When D wants to share the secret K among the participants in E , D gives each
93 participant some partial information, called a share. The shares are distributed secretly, so no participant knows
94 any other participant's share.

95 At a later time, when some qualified subset of participants $F \subseteq E$ want to compute the secret K , they will
96 then pool their shares together. The most famous construction of a (t, n) -threshold scheme, called the Shamir
97 Threshold Scheme [18][21], is invented in 1979. Therefore, a (t, n) threshold secret sharing scheme can protect the
98 secret against an adversary who can intercept at most $t-1$ paths. In t he proposed model D don't want to share
99 the secret K among several participants in E , but D wants to share the key with the other end of communication
100 say G , with whom he wants a secure communication. So D sends the shares of thee : $A_1 \times A_2 \subseteq C$. $1 \leq O \leq X$
101 $\leq A_1 Y \leq A_2 Y \leq A_2 O X, X_1, X_2 \leq A_1$, and $Y, Y_1, Y_2 \leq A_2$ and $u, v \leq Z$ we have $e(X_1 + X_2, Y_1)$

102 $= e(X_1, Y_1) e(X_2, Y_1), e(X_1, Y_1 + Y_2) = e(X_1, Y_1) e(X_1, Y_2)$. $e([u]X, [v]Y) = e(X, Y) uv =$
103 $e([v]X, [u]Y)$.

104 where $[u]X = X + X + \dots + X$ (u times)? A 1 and Y ? A 2 .

105 ?A 1 , and Y ? [11] and Tate Pairing [5]. Pairings in elliptic curve cryptography are functions which map a
106 pair of elliptic curve points to an element of the multiplicative group of a finite field. A 2 and u, v ? Z and O $e(X,$
107 $O) = e(O, Y) = 1$ $e(-X, Y) = e(X, -Y) e([u]X, Y) = e(X, Y) u = e(X, [u]Y) e([u]X, [v]Y) = e(X,$
108 $Y) uv e : A 1 \times A 1 ? C, A 1 A 1 ? A 2 ? : A 2 ? A 1 ; A 1 ? A 2$

109 There are two types of pairings commonly used in the cryptography literature. The first type of pairing called
110 Symmetric Pairings are of the form secret key K through n independent paths [24] to G. When G receives at
111 least t shares, he can recover the secret and there by a key is shared between D and E.

112 Year 2015 $e : A 1 \times A 2 ? C$, where A1, A2 are additively written cyclic groups of prime order p and C is a
113 multiplicatively written cyclic group of prime order p.

114 The opponent is facing the challenge of getting at least t shares by intercepting t paths at the same time,
115 unless until he cannot recover the secret key.

116 6 III.

117 7 Related Work

118 There are many key agreement protocols based on bilinear maps, and later most of them have been broken.
119 One of the first applications of pairing based cryptography was a tripartite key agreement protocol given by
120 Joux [1]. This key agreement protocol does not authenticate the users, and thus is subject to the attack namely
121 man-in-the-middle. Of course, it was an important step in the advancement of pairing based cryptography. This
122 protocol only uses pairings especially Tate pairing but does not use identity-based cryptography.

123 Many key agreements from bilinear maps and identity based cryptography have been since proposed. Scott
124 [7], Smart [8], and Chen and Kudla [6] have proposed two-party key agreement protocols, none of which have
125 been broken. All of these schemes require that all parties involved in the key agreement are clients of the same
126 Key Generation Centre (KGC). Nalla recommends a tripartite identity-based key agreement in [9], and Nalla
127 and Reddy recommends a authenticated tripartite identity-based key agreement scheme in [10], but both have
128 been broken down [12,13]. Shim presents two key agreement protocols [14,15], but both of these schemes have
129 been broken by Sun and Hsieh [16]. Another authenticated tripartite key agreement protocol recommended by
130 Al-Riyami and Patterson [3] was broken by Shim [4]. Cullagh and Barreto recommend a two-party identity based
131 authenticated key agreement. Most of the above protocols are based on identity-based cryptography.

132 Our proposed model is based on Joux's Protocol [1]

133 8 b) Diffie-Hellman Assumption

134 In this subsection we specify the version of the Diffie-Hellman problem which we will require. Consider the triple
135 $\langle A, C, e \rangle$ where A , C are two cyclic subgroups of a large prime order q and $e : A1 \times A ? C$ is a cryptographic
136 bilinear map. We take A as an additive group and C as a multiplicative group.

137 9 Bilinear Diffie-Hellman BDH Problem

138 The strength of Joux's protocol is based on the Bilinear Diffie-Helman (BDH) [2] assumption. Let P be the
139 generator of A1 and a, b, c are positive integers . The BDH assumption considers the computation of $e(P, P)$
140 given $\langle P, aP, bP, cP \rangle$ to be hard. When A and B receives at least t shares of Si and Ri respectively, they
141 can reconstruct S and R as Hence unless the adversary intercepts at least t shares of Ri and Si, he cannot
142 reconstruct R and S and therefore the key. Also the key is the session key that has small life time i.e., over a
143 single session; hence the time scope for adversary to reconstruct the key is small, thereby protecting the protocol
144 from man-in-the-middle attack.

145 10 c) Man-in-the-middle Attack

146 V.

147 11 Implementation

148 The proposed key agreement protocol is implemented in software using the Pairing-Based Cryptography Library
149 (PBC) ??20]. The results are as follows: The Elliptic curve is chosen as: $y^2 = x^3 + x$, with x, y elements of a
150 Field F_q ; q is a prime number. A1 is a subgroup of $E(F_q)$. C is a subgroup of F_{q^2} . There Year 2015

151 To counter this we apply the concept of threshold cryptography for steps 1 and 2; steps 3 and 4 remain the
152 same. The secrets 'u' and 'v' are split into n shares each using Shamir's secret sharing mechanism [21] to get
153 u_i and v_i where n is the number of multiple independent paths that exist between sender and receiver. The
154 shares of the products $[u]P$ and $[v]P$ are then calculated as $R_i = [u_i]P$ and $S_i = [v_i]P$. These shares are then
155 exchanged through n independent paths with the other party as shown in

156 12 Conclusion and Future Scope

157 In this article, we described a generalization of the Diffie-Hellman protocol and Joux Protocol to two parties. Our
158 two-party key agreement protocol uses the pairings and threshold cryptography concepts. Our model also does
159 not assume a centralized trusted authority, which is difficult to establish in MANET environment. Therefore, this
160 new protocol seems quite promising as a new building block to construct new and efficient complex cryptographic
161 protocols. On the other hand, there is a scope to ensure the integrity of the secret shares. Additionally, there
162 is scope to use this shared secret key in pairing based cryptography for encryption and decryption of messages,
there by secret transmission of messages between the two communicating parties. ¹



163 Figure 1: 1 2E

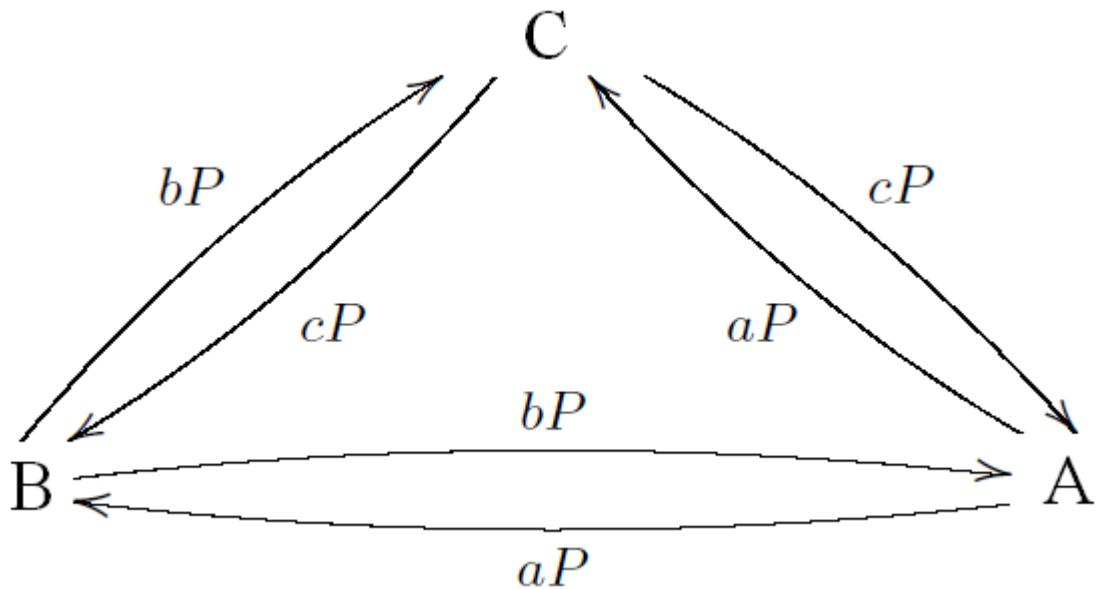


Figure 2:

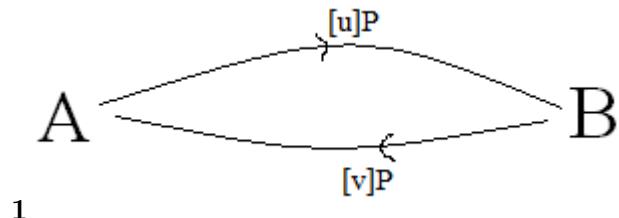
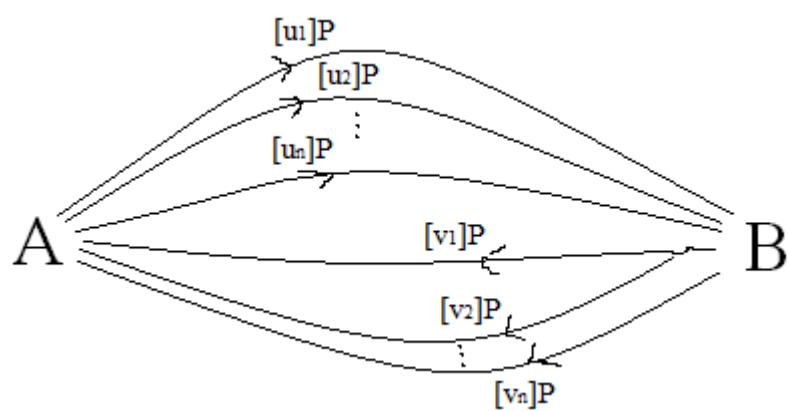


Figure 5: Figure 1 :



231

Figure 7: Figure 2 :Figure 3 : 1 4

$\Sigma_{\mathbf{q}, \alpha}^X$

Figure 8:

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